#### References

- K. Wakino et al., "Microwave bandpass filters containing dielectric resonators with improved temperature stability and spurious response," in *Proc. IEEE Int. Microwave Symp.*, Palo Alto, CA, pp. 63-65, May 1975.
   D. J. Masse et al., "A new low-loss high-ε, temperature com-
- [2] D. J. Masse et al., "A new low-loss high-ε, temperature compensated dielectric for microwave applications," Proc. IEEE, vol. 59, pp. 1628–1629, Nov. 1971.
- [3] M. W. Pospieszalski, "Cylindrical dielectric resonators and their applications in TEM line microwave circuits," *IEEE Trans. Micro*wave Theory Tech., vol. MTT-27, pp. 233–238, Mar. 1979.
- [4] A. Karp, H. J. Shaw, and D. K. Winslow, "Circuit properties of microwave dielectric resonators," *IEEE Trans. Microwave Theory Tech.*, vol. MTT-16, pp. 818–829, Oct. 1968.
- [5] S. Fiedziuszko and A. Jeleński, "The influence of conducting walls on resonant frequencies of the dielectric resonator," *IEEE Trans. Microwave Theory Tech.*, vol. MTT-19, p. 778, Sept. 1971.
- [6] T. Itoh and R. Rudokas, "New method for computing the resonant frequency of dielectric resonator," *IEEE Trans. Microwave Theory Tech.*, vol. MTT-25, pp. 52-54, Jan. 1977.
- [7] J. van Bladel, "On the resonances of a dielectric resonator of very high permittivity," *IEEE Trans. Microwave Theory Tech.*, vol. MTT-23, pp. 199-208, Feb. 1975.

- [8] —, "The excitation of dielectric resonators of very high permittivity," *IEEE Trans. Microwave Theory Tech.*, vol. MTT-23, pp. 208-218, Feb. 1975.
- [9] S. H. Gould, Variational Methods for Eigenvalue Problems. Toronto, Canada: Univ. of Toronto Press, 1966.
- [10] M. Jaworski, "On the resonant frequency of a re-entrant cylindrical cavity," *IEEE Trans. Microwave Theory Tech.*, vol. MTT-26, pp. 256-260, Apr. 1978.
- [11] —, "Resonant cavity Method for the Determination of Complex Permittivity", (in Polish), Ph.D. dissertation, Inst. of Phys., Polish Academy of Sciences, Warsaw, Poland, 1976.
- [12] R. F. Harrington, *Time Harmonic Electromagnetic Fields*. New York: McGraw-Hill, 1961.
- [13] —, Field Computation by Moment Methods. New York: MacMillan, 1968.
- [14] B. Friedman, Principles and Techniques of Applied Mathematics. New York: Wiley, 1956.
- [15] Y. Konishi, N. Hoshino, and Y. Utsumi, "Resonant frequency of a TE<sub>018</sub> dielectric resonator," *IEEE Trans. Microwave Theory Tech.*, vol. MTT-24, pp. 112-114, Feb. 1976.
- [16] P. Guillon and Y. Garault, "Accurate resonant frequencies of dielectric resonators," *IEEE Trans. Microwave Theory Tech.*, vol. MTT-25, pp. 916–922, Nov. 1977.

# Design of Microwave GaAs MESFET's for Broad-Band Low-Noise Amplifiers

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Abstract—As a basis for designing GaAs MESFET's for broad-band low-noise amplifiers, the fundamental relationships between basic device parameters, and two-port noise parameters are investigated in a semiempirical manner. A set of four noise parameters are shown as simple functions of equivalent circuit elements of a GaAs MESFET. Each element is then expressed in a simple analytical form with the geometrical and material parameters are developed in terms of the geometrical and material parameters.

Among the four noise parameters, the minimum noise figure  $F_{\rm min}$ , and equivalent noise resistance  $R_n$ , are considered crucial for broad-band low-noise amplifiers. A low  $R_n$  corresponds to less sensitivity to input mismatch, and can be obtained with a short heavily doped thin active channel. Such a high channel doping-to-thickness (N/a) ratio has a potential of producing high power gain, but is contradictory to obtaining a low  $F_{\rm min}$ . Therefore, a compromise in choosing N and a is necessary for best overall amplifier performance. Four numerical examples are given to show optimization processes.

#### I. INTRODUCTION

T HE GaAs Schottky-barrier gate field effect transistors (GaAs MESFET's) have demonstrated excellent noise and gain performance at microwave frequencies

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through K band [1]. The excellent microwave performance of GaAs MESFET's is certainly related to their channel properties. GaAs MESFET's to be used for broad-band low-noise amplifier applications, must have special requirements on their channel properties for optimum performance. The purpose of this paper is to investigate the fundamental relationships between the noise and smallsignal properties, and the basic channel parameters of GaAs MESFET's. This information should be useful as a basis for device design.

#### II. REPRESENTATION OF NOISE PROPERTIES

## A. Noise Parameters

From the circuit point of view, the GaAs MESFET can be treated as a black box of noisy two port. The noise properties of such a black box are then characterized by a set of four noise parameters in the binomial form [2]. A derivation of this form can be written as

$$F = F_{\min} + \frac{R_n}{R_{ss}} \left[ \frac{(R_{ss} - R_{op})^2 + (X_{ss} - X_{op})^2}{R_{op}^2 + X_{op}^2} \right]$$
(1)

where

F	noise figure,
$F_{ m min}$	minimum (or optimum) noise figure,
$R_n$	equivalent noise resistance,
$R_{ss}$	signal source resistance,
R <sub>op</sub>	optimum signal source resistance,
$R_{op} \ X_{ss}$	signal source reactance,
$X_{op}$	optimum signal source reactance.
-1	

In this expression,  $F_{\min}$ ,  $R_n$ ,  $R_{op}$ , and  $X_{op}$  are the characteristic noise parameters of the device. Since the noise figure F is a function of its driving source impedance, the minimum noise figure  $F_{\min}$  is achieved only when the driving source impedance is exactly at the optimum signal source impedance.

As has been well known, (1) can be represented on the source impedance Smith chart as a family of circles, each of which corresponds to a constant F value [3]. The spatial distance between two circles is related to  $R_n$ . The greater  $R_n$  corresponds to the shorter distance. In other words, the noise figure of a device with a small value of  $R_n$  is relatively insensitive to the variation in the signal source impedance. Thus small  $R_n$  is essential for a device to be used in a broad-band amplifier where a large tolerance is desirable in the input match. Furthermore, as will be seen later,  $R_n$  has a close relationship with power gain. Usually, the smaller  $R_n$  value corresponds to the higher gain in a given gate structure. In the design of a low-noise MESFET, therefore, obtaining a low  $R_n$  should be considered to be just as crucial as achieving a low  $F_{min}$ .

It may be noted that an equivalent expression of (1), in terms of the source-reflection coefficient, is found elsewhere [4]. This expression is based on the circuit analysis using the *s* parameters. The *s*-parameter representation would be convenient to use in conjunction with the test facilities available for two-port investigation these days. However, the impedance parameter would provide us with direct insight into the operation of a device under consideration. Therefore, the noise parameters in the impedance form are adopted in this paper. If necessary, the noise parameters of this form can be transformed into other forms in a straightforward manner.

## B. Noise Equivalent Circuit

It has been well accepted that the noise properties of a GaAs MESFET would be described by an equivalent circuit as shown in Fig. 1 [5], if the effect of reactive parasitic elements on the noise performance could be ignored. The major reactive parasitic elements are lead inductances and header stray capacitances. As the operating frequency increases, the impedance of such external elements may become comparable to those of the corresponding internal elements, and then the reactive parasitic effects are no longer negligible. Such a critical frequency, that the reactive parasitic effect begins to participate in the determination of the noise performance parameters, may vary from one noise parameter to another for a given



Fig. 1. Noise equivalent circuit of GaAs MESFET's.  $g_m$  is the transconductance which is assumed to be constant over the frequency range of interest. Element  $C_{gs}$  is the gate-source capacitance,  $r_i$ , the associated charging resistance,  $R_g$ , the ac gate metallization resistance, and  $R_s$ , the total source resistance series. Noise sources  $i_{ng}$ ,  $i_{nd}$ ,  $e_{ng}$ , and  $e_{ns}$  represent the induced gate noise, drain-circuit noise, thermal noise of  $R_g$ , and  $R_s$ , respectively.

device. For example, the critical frequency for  $F_{\min}$  may be much higher than those for  $R_n$ ,  $R_{op}$ , and  $X_{op}$ , analogous to microwave bipolar transistors [6].

# III. FORMULATION OF NOISE PARAMETERS IN TERMS OF DEVICE GEOMETRICAL AND MATERIAL PARAMETERS

# A. Experimental Procedure and Results

Relationships between the noise parameters and equivalent circuit elements have been given in rigorous but complicated forms [5]. For practical purposes, however, it would be much more convenient if simple analytical forms of such relationships were available with reasonable accuracy.

In order to carry out this search, GaAs MESFET's with nominal gate length of 2  $\mu$ m were used in the experiments described below. The MESFET's were mounted in the package which had a total input lead inductance of approximately 1 nH, a total output lead inductance of approximately 1 nH, a common-source lead inductance of approximately 0.12 nH, and a header stray capacitance of approximately 0.08 pF at both input and output [7]. As a result of such parasitic element values, these devices nearly satisfied the aforementioned requirement for possible elimination of the reactive parasitic effects on any of the four noise parameters at a test frequency of 1.8 GHz. Therefore, only the equivalent circuit elements shown in Fig. 1 will be referred to in the analyses described later on.

Table I shows the geometrical and material parameters of the six GaAs MESFET's used in the experiments. In Table I, N is the free carrier concentration in the active channel in units of  $10^{16}$  cm<sup>-3</sup>, L is the gate length in micrometers, a is the active channel thickness in micrometers, Z is the total device width in millimeters, and z is the unit gate width in millimeters. Since z was 0.25 mm for all devices, each device had either two or six paralleled unit

TABLE I
GEOMETRICAL AND MATERIAL PARAMETERS OF SAMPLE GaAs
MESFET's

		DEVICE	$(10^{16} \text{cm}^{-3})$	L (µm)	a (µm)	Z (mm)	2 (mm)
a	:	K864-1-02	11.0	1.85	0.174	0.5	0.25
b :		K976-1-04	7.5	1.85	0.40	0.5	0.25
с		K949 <b>-1-</b> 12	5.5	1.85	0.44	0.5	0.25
d :	:	к949-3-02	5.5	2.3	0.35	1.5	0.25
е :	:	C75B <b>-</b> 1-05	5.0	2.3	0.46	0.5	0.25
f :		с <b>75в-3-0</b> 4	5.0	2.3	0.38	1.5	0.25

TABLE II Measured Values of Noise Parameters and Equivalent Circuit Elements of Sample GaAs MESFET's

DEVICE	F <sub>min</sub> (dB)	R <sub>n</sub> (Ω)	R <sub>op</sub>	X <sub>op</sub> (Ω)	ខ <sub>m</sub> (ប)	C <sub>gs</sub> (pF)	R <sub>g</sub> (∩)	R <sub>s</sub> (Ω)
а	1.80	31	40	85	0.031	1.0	2	8.5
b	1.29	-	45	145	0.021	0.65	2	6
с	1.56	-	45	140	0.019	0.62	3	6
d	1.70	13.3	23	47	0.047	2.0	1	3.5
е	1.73	94	50	125	0.018	0.68	2	8
f	2.04	15.3	35	45	0.044	2.2	4	3.5

gates. These devices were an early version of the low-noise GaAs MESFET reported elsewhere [8]. An epitaxial film, as the active channel, was grown directly on a semi-insulating substrate in the first four devices. In the last two devices, however, there was an additional undoped buffer layer between the substrate and active layer.

Four noise parameters  $F_{\min}$ ,  $R_n$ ,  $R_{op}$ , and  $X_{op}$  were measured at 1.8 GHz under optimum gate-bias condition for each device, using the standard technique [9]. Equivalent circuit elements  $g_m$ ,  $C_{gs}$ ,  $R_g$ , and  $R_s$  were evaluated from the *s*-parameter measurement taken as a function of frequency under the zero gate-bias condition, in a similar way to that described in [10]. All the above parameters were measured at room temperature. The results are shown in Table II.

## B. Derivation of Expressions for Noise Parameters in Terms of Equivalent Circuit Elements

It was assumed that the four noise parameters could be expressed in terms of equivalent circuit elements as follows:

$$F_{\min} = 1 + k_1 f C_{gs} \sqrt{\frac{R_g + R_s}{g_m}}$$
(2)

$$R_n = \frac{k_2}{g_m^2} \tag{3}$$



Fig. 2. Correlation between the minimum noise figure  $F_{\min}$  and equivalent circuit elements,  $C_{gs}$ ,  $g_m$ ,  $R_g$ , and  $R_s$ .



Fig. 3. Correlation between the equivalent noise resistance  $R_n$  and transconductance  $g_m$ .

$$R_{op} = k_3 \left[ \frac{1}{4g_m} + R_g + R_s \right] \tag{4}$$

$$X_{op} = \frac{k_4}{fC_{gs}} \tag{5}$$

where  $k_1$ ,  $k_2$ ,  $k_3$ , and  $k_4$  are fitting factors, and f is frequency.

Comparing these expressions with the experimental data shown in Table II would yield determination of the fitting factors. As seen in Figs. 2-5, it has been found that the expressions would well represent the measured values of the noise parameters if the fitting factors were chosen as follows:

$$k_1 = 0.016$$
  
 $k_2 = 0.030$ 



 $1/4g_{m}+R_{g}+R_{s}$  ( $\Omega$ )

Fig. 4. Correlation between the optimum source resistance  $R_{op}$  and equivalent circuit elements  $g_m$ ,  $R_g$ , and  $R_s$ .



Fig. 5. Correlation between the optimum source reactance  $X_{op}$  and gate-source capacitance  $C_{gs}$ .

$$k_3 = 2.2$$
  
 $k_4 = 160$ 

provided that  $R_n$ ,  $R_{op}$ ,  $X_{op}$ ,  $R_g$ , and  $R_s$  are all in ohms,  $g_m$  in mhos,  $C_{gs}$  in picofarads, and f in gigahertz.

It may be remarked that the equivalent circuit elements as obtained with null gate bias are used in the above expressions for the noise parameters, although the noise parameters are provided with a certain gate bias. In spite of such a difference in the gate-bias conditions, the above relationships were empirically found to be present. If the equivalent circuit elements were measured under a gatebias condition different from the null gate bias, the fitting factors would have to be modified.

A deviation of  $X_{op}$ , with increasing  $C_{gs}$ , from the linear relationship as seen in Fig. 5 was probably caused by an increased participation of the input lead inductance in  $X_{op}$ .

# C. Semiempirical Expressions for Transconductance, Gate-Source Capacitance, and Cutoff Frequency

For design purposes,  $g_m$  and  $C_{gs}$  must be expressed in terms of the geometrical and material parameters of a device. Approximate expressions were then derived on a semiempirical basis as follows:

$$g_m = k_5 Z \left[ \frac{N}{aL} \right]^{1/3} \mathfrak{V} \tag{6}$$

$$C_{gs} = k_6 Z \left[ \frac{NL^2}{a} \right]^{1/3} \text{pF}$$
(7)

$$f_T = \frac{10^3 g_m}{2\pi C_{gs}} = \frac{9.4}{L} \text{ GHz}$$
 (8)

in which fitting factors  $k_5$  and  $k_6$  were found to be 0.020 and 0.34, respectively, for the sample devices under the zero gate-bias condition.

Figs. 6 and 7 show comparisons of  $g_m$  and  $C_{gs}$ , respectively, between the calculated values using L, N, and a given in Table I and the measured values shown in Table II. They are in good agreement in both cases.

## D. Simplified Expressions for Parasitic Resistances

Simplified expressions for  $R_g$  and  $R_s$  of the sample MESFET's would be given by [11]

$$R_g = \frac{17z^2}{hLZ} \ \Omega \tag{9}$$

$$R_s = \frac{1}{Z} \left[ \frac{2.1}{a^{0.5} N^{0.66}} + \frac{1.1 L_{sg}}{(a - a_s) N^{0.82}} \right] \Omega$$
(10)

where h is the gate metallization height in micrometers,  $L_{sg}$  is the distance between the source and gate electrodes in micrometers, and  $a_s$  is the depletion layer thickness in micrometers at the surface in the source-gate space.

## E. Practical Expressions for Noise Parameters

The substitution of (6)-(10) into (2)-(5) in association with the practical values of the fitting factors yields

$$F_{\min} = 1 + 0.038 f \left[ \frac{NL^5}{a} \right]^{1/6} \cdot \left[ \frac{17z^2}{hL} + \frac{2.1}{a^{0.5}N^{0.66}} + \frac{1.1L_{sg}}{(a-a_s)N^{0.82}} \right]^{1/2}$$
(11)

$$R_n = 75Z^{-2} \left[ \frac{aL}{N} \right]^{2/3} \Omega \tag{12}$$

$$R_{op} = 2.2Z^{-1} \left[ 12.5 \left( \frac{aL}{N} \right)^{1/3} + \frac{17z^2}{hL} + \frac{2.1}{a^{0.5}N^{0.66}} + \frac{1.1L_{sg}}{(a-a_s)N^{0.82}} \right] \Omega \quad (13)$$



Fig. 6. Transconductance  $g_m$  as a function of channel parameters Z, L, a, and N.



Fig. 7. Gate-source capacitance  $C_{gs}$  as a function of channel parameters Z, L, a, and N.

$$X_{op} = \frac{450}{fZ} \left[ \frac{a}{NL^2} \right]^{1/3} \Omega.$$
 (14)

Again, units are gigahertz (GHz) for f, millimeter (mm) for z and Z, micrometer ( $\mu$ m) for a,  $a_s$ , h, L, and  $L_{sg}$ , and  $10^{16}$  cm<sup>-3</sup> for N.

Since  $F_{\min}$  is dominated by the parasitic resistances outside the gate region,  $F_{\min}$  is structure sensitive [12]. Remember that (11) is suitable for the simplest structure of MESFET's. As sophistication increases in the structure, the proper expression for  $F_{\min}$  may be obtained after the corresponding modification primarily to (10), and hence to (11). Applications of the gate recess structure [8], [12] and n<sup>+</sup>-GaAs epitaxial layer [13] are the major examples of structural variations so far reported.

In (12), it is seen that a small  $R_n$  value can be obtained with a short gate device having a heavily doped thin active channel. The expression for  $R_n$  given in (12) may hold, regardless of the structural modification applied to a section of the channel outside the gate region.

# IV. DISCUSSIONS ON MINIMUM NOISE FIGURE, Associated Power Gain, and Input Impedance Match

# A. Example 1

In order to see the characteristic variations of  $F_{\min}$  and  $R_n$  as functions of N and a, the following conditions are assumed:

$$L = L_{sg} = 1.0 \ \mu \text{m}$$
  
 $R_g = 4.0 \ \Omega$   
 $f = 0.4 f_T = 3.76 \text{ GHz}.$ 

Furthermore,  $a_s$  is assumed to be approximately equal to the gate depletion layer thickness under null gate-bias condition  $a_0$  in numerical value. This parameter has been given by [11]

$$a_0 = \left[\frac{0.706 + 0.06 \log N}{7.23N}\right]^{1/2} \mu m$$

for aluminum gates, as far as  $a > a_0$ . Under such conditions, (11) reduces to

$$F_{\min}|_{f=0.4f_T} = 1 + 0.15 \left[ N/a \right]^{1/6} \cdot \left[ 1.82 + \frac{1.9}{a^{0.5}N^{0.66}} + \frac{1}{(a-a_0)N^{0.82}} \right]^{1/2}.$$
 (15)

The calculated values of  $F_{\min}$  by (15) and of  $R_n$  by (12) are shown in Fig. 8, both as the contour mapping on the *a-N* plane. It can be seen that  $F_{\min}$  is a weak function of *N* for a given value of *a*. Also,  $F_{\min}$  takes a low value in the region where the a/N ratio is high. This is the contradictory condition to obtaining the low value of  $R_n$ . The high a/N ratio tends to provide not only the critical noise tuning but also the low power gain. Therefore, there is a compromise in choosing *a* and *N* for the best overall performance as an amplifying device.

In Fig. 8, there are two other curves, as shown with the dash-dotted line, which indicate practical limits for the selection of a and N. The upper curve corresponds to the a and N values which provide a drain-source breakdown voltage  $V_B$ , of 10 V if the gate is biased at the pinchoff voltage,  $-V_p$ . The lower curve indicates the thickness of the gate depletion layer at zero bias for aluminum gates.

#### B. Example 2

In order to see a clear distinction between the low a/N device and high a/N device, the following two representatives were assumed under the same conditions, as used in the previous section.

Device A: 
$$N = 12.5 \times 10^{16} \text{ cm}^{-3}$$
 and  $a = 0.2 \,\mu\text{m}$ .  
Device B:  $N = 5.0 \times 10^{16} \text{ cm}^{-3}$  and  $a = 0.5 \,\mu\text{m}$ .

The noise performance of these devices was calculated using (12)-(15). The results are then plotted on the signal



Fig. 8. Contours of equi- $F_{\min}$  and equi- $R_n$  on the *a*-N plane for 1- $\mu$ m gate devices.

$L = L_{sa} = 1 \mu m$	DEVICE	N(10 <sup>16</sup> cm−3)	a(μm )
Z = 0.5mm, z=0.25mm	A	12.5	0.2
R <sub>g</sub> =4Ω, f= 3.8 GHz	—— В	5.0	0.5
$Z_0 = 50\Omega$			



Fig. 9. The noise performance chart for two 1-µm gate devices.

source impedance chart [3], as shown in Fig. 9. It may be concluded that device B may reach the better noise performance in the case of a narrow-band application with the individually designed circuitry. However, device Amay be more suitable in such a case that relatively large tolerances for the impedance variation are demanded. In addition, device A usually gives gain higher than that of device B, because of the higher value of  $g_m$  with device A.

### C. Example 3

As seen in Fig. 9, device *B*, in spite of the smaller value of  $F_{\min}$ , would exhibit much worse noise figure than



Fig. 10. Noise figures  $F_{\min}$  and  $F_{50}$  as functions of total device width Z for two 1- $\mu$ m gate devices.

device A when they are simply inserted into a 50- $\Omega$  coaxial system. Such a 50- $\Omega$  system insertion noise figure can be designated as  $F_{50}$ , which is

$$F_{50} = F_{\min} + \frac{R_n}{50} \left[ \frac{(50 - R_{op})^2 + X_{op}^2}{R_{op}^2 + X_{op}^2} \right].$$
 (16)

Next shown are the dependence of  $F_{\min}$  and  $F_{50}$  on Z, provided that Z = 2z. Two representative devices C and D were chosen, which were the same as devices A and B, respectively, except for an additional assumption that  $R_g = 8Z$ , in which  $R_g$  is in units of ohms and Z is in millimeters. Parameters  $F_{\min}$  and  $F_{50}$  were then calculated as functions of Z, using (11)-(14) and (16). The results are shown in Fig. 10, in which  $F_{\min}$  gradually increases with increasing Z for both devices. On the contrary,  $F_{50}$  varies as a strong function of Z and takes a minimum for moderate values of Z, as also shown in Fig. 10. For the overall performance as a general purpose low-noise MESFET with two paralleled unit-gates 1  $\mu$ m long, an optimum value of the total gate width could be evaluated to be 0.4-0.5 mm for device C, and 0.8-1.0 mm for device D.

## D. Example 4

In [14], the noise and gain performance as measured at 8 GHz for GaAs MESFET's with 0.5- $\mu$ m-long gates was described. The device consists of four sections of 70- $\mu$ m-wide units, i.e., z = 0.07 mm and Z = 0.28 mm. The height of aluminum as the gate metallization was 0.5  $\mu$ m. The source-to-gate distance was 0.8  $\mu$ m. The active layer thickness was claimed to be between 0.1 and 0.2  $\mu$ m. The gate pinchoff voltage  $V_p$  of typical devices was 2.0 V. Since the representative value of N was  $25 \times 10^{16}$  cm<sup>-3</sup>, the corre-



Fig. 11. Calculated values of  $F_{\min}$  and measured values of  $F_{\min}$  and associated power gain  $G_a$  for 0.5- $\mu$ m gate devices.

sponding value of a was evaluated to be 0.124  $\mu$ m. Thus  $F_{\min}$  at 8 GHz was calculated using (11) as a function of N for the three values of a, i.e., 0.1, 0.124, and 0.2  $\mu$ m.

As shown in Fig. 11, the measured  $F_{\rm min}$  values happened to be between the two calculated curves of  $F_{\rm min}$ for a=0.1 and 0.2  $\mu$ m. Moreover, the measured  $F_{\rm min}$  for  $N \ge 10 \times 10^{16}$  cm<sup>-3</sup> agreed well with the calculated  $F_{\rm min}$ for  $a=0.124 \ \mu$ m. However, the measured  $F_{\rm min}$  for  $N < 10 \ \times 10^{16}$  cm<sup>-3</sup> appeared to be better than the calculated  $F_{\rm min}$  for  $a=0.124 \ \mu$ m. This discrepancy could have been caused by an increased active layer thickness of the actual devices with  $N < 10 \times 10^{16}$  cm<sup>-3</sup>, in order to maintain the zero gate-bias drain current to be finite in the positive direction. Such an increase in a should result in an improvement of  $F_{\rm min}$  from that predicted for  $a=0.124 \ \mu$ m, as seen in Fig. 11. Therefore, it can be concluded that the experimental data on the noise performance, [14, fig. 2], is well explained by (11) of this paper.

In the same reference figure as mentioned above the associated power gain  $G_a$ , was also shown as a function of N. The data are replotted in Fig. 11 in which  $G_a$  increases with increasing N and hence N/a, as has been predicted in the previous sections of this paper.

## E. Remarks

In general, with increasing N/a,  $G_a$  increases and  $R_n$  decreases. If  $R_g$  is small enough as compared to  $R_s$ ,  $F_{mun}$  is

improved with an increased value of N for a given value of a. This has been empirically known in the industry [15]. The reason is that  $R_s$  dominates  $F_{\min}$  for a given value of L, and that  $R_s$  decreases with increasing the Na product. In the simple planar channel structure used here,  $F_{\min}$ increases with decreasing a for a given N. However, in a sophisticated channel structure, this may no longer hold partly due to a possible decrease in the effective gate length [11], [13].

### V. CONCLUSIONS

A set of four noise parameters for GaAs MESFET's of the planar channel structure were semiempirically found in terms of simple functions of its equivalent circuit elements. Each of the equivalent circuit elements was further expressed by the device geometrical and material parameters in a simple analytical form. Combining these two things together yielded the practical expressions for the four noise parameters in terms of the device geometrical and material parameters.

Among the four noise parameters,  $F_{\min}$  and  $R_n$  were regarded as most crucial for a device to be used in a broad-band low-noise amplifier. Because a device with a small value of  $R_n$  behaves rather insensitively to the variation in the signal source impedance, the variation in the noise figure over the band can be expected to be small. In addition, as the inverse of  $R_n$  is closely related to power gain, smaller  $R_n$  can enhance the gain performance.

The aforementioned expression for  $R_n$  indicates that a small value of  $R_n$  can be obtained with a short gate device having a heavily doped thin active channel (i.e., a high N/a ratio). This is, in general, the contradictory condition to obtaining a low value of  $F_{\min}$ . Although  $F_{\min}$  is a weak function of N for a given value of a,  $F_{\min}$  takes a low value in the region where the N/a ratio is low. However, the low N/a ratio tends to make the noise tuning critical and to degrade the power gain. Therefore, a compromise in choosing a and N is necessary for the best overall amplifier performance.

The proper selection of a and N may vary depending upon the particular purpose of an amplifier. Four examples were given to show the dependence of the noise, gain and input matching properties on a and N in a practical manner. If the gate metallization resistance were designed to be small enough to the total source series resistance, the minimum noise figure, associated power gain, and input matching sensitivity would all be improved with increasing N for a given a. This is a case which has been often observed in the industry.

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#### References

- H. F. Cooke, "Microwave FET's—A status report," in IEEE ISSCC Dig. Tech. Papers, 1978, pp. 116–117.
- [2] H. Rothe and W. Dahlke, "Theory of noisy fourpoles," Proc. IRE, vol. 44, pp. 811-818, June 1956.
- [3] H. Fukui, "Available power gain, noise figure, and noise measure of twoports and their graphical representation," *IEEE Trans. Circuit Theory*, vol. CT-13, pp. 137-142, June 1966.
- [4] J. A. Eisenberg, "Systematic design of low-noise, broad band microwave amplifiers using three terminal devices," in *Microwave* Semiconductor Devices, Circuits and Applications, Proc. Fourth Cornell Conf., 1973, pp. 113-122.
- [5] R. A. Pucel, H. A. Haus, and H. Statz, "Signal and noise properties of gallium arsenide microwave field-effect transistors," in *Advances in Electronics and Electron Physics*. New York: Academic, vol. 38, 1975, pp. 195-265.
- [6] H. Fukui, "The noise performance of microwave transistors," *IEEE Trans. Electron Devices*, vol. ED-13, pp. 329-341, Mar. 1966.
- [7] W. O. Schlosser, private communication.
- [8] B. S. Hewitt et al., "Low-noise GaAs M.E.S.F.E.T.S.," Electron.

Lett., vol. 12, pp. 309-310, June 10, 1976.

- [9] "IRE Standards on Electron Tubes: Methods of Testing," 1962, 62 IRE 7 S1, pt. 9: Noise in linear twoports.
- [10] J. Jahncke, "Höchstfrequenzeigenshaften eines GaAs MESFET's in Steifenleitungstechnik," Nachrichtentech. Z., vol. 5, pp. 193–199, May 1973.
- [11] H. Fukui, "Determination of the basic device parameters of a GaAs MESFET," *Bell Syst. Tech. J.*, vol. 58, pp. 771-797, Mar. 1979.
- [12] B. S. Hewitt et al., "Low-noise GaAs MESFET's: Fabrication and performance," in Gallium Arsenide and Related Compounds (Edinburg) 1976, Conf. Series No. 33a, The Inst. Physics, Bristol and London, 1977, pp. 246-254.
- [13] H. Fukui, "Optimal noise figure of microwave GaAs MESFET's," *IEEE Trans. Electron Devices*, vol. ED-26, pp. 1032–1037, July 1979.
- [14] M. Ogawa, K. Ohata, T. Furutsuka, and N. Kawamura, "Submicron single-gate and dual-gate GaAs MESFET's with improved low noise and high gain performance," *IEEE Trans. Microwave Theory Tech.*, vol. MTT-24, pp. 300–306, June 1976.
- [15] H. F. Cooke, "Microwave field effect transistors in 1978," Microwave J., vol. 21, no. 4, pp. 43–48, Apr. 1978.

# Continuous Varactor-Diode Phase Shifter with Optimized Frequency Response

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Abstract—A method is introduced for designing continuous varactordiode phase shifters with optimum frequency response. The circuit used gives very small frequency variations of the phase shift if the maximum phase shift of the device is less than about 200°. Measurement results on a 180° *L*-band phase shifter are presented. This unit gives less than 5° variation of any given phase shift less than 180°, when the frequency is changed from 1.5 to 1.7 GHz.

### I. INTRODUCTION

A PROBLEM in the design of continuous varactordiode phase shifters which has not received previous attention is the optimum frequency behavior at all possible phase shifts. The frequency response is said to be optimum when the derivative of the phase shift with frequency is zero at the center frequency. In this paper the design of a 180° continuous phase shifter will be described, which is almost ideal in this respect. An interesting  $360^{\circ}$  varactor-diode phase shifter was introduced in 1971 by Henoch and Tamm [1]. The main parts of the design were two parallel coupled series resonant circuits which were connected to a circulator by means of a quarter-wave transformer. The purpose of the transformer was to equalize the insertion loss. The phase shifter was designed to give optimum frequency behavior at  $360^{\circ}$  phase shift, but computer simulation has shown large frequency dependence at phase shifts between  $0^{\circ}$ and  $360^{\circ}$ .

Starski [2] has reported on an increase in bandwidth for p-i-n-diode reflection-type phase shifters by choosing the length and the impedance of the transformer for optimum frequency response. An attempt was made to improve the continuous 360° shifter in this way, but it was not possible to decrease the frequency variations at all phase shifts to any large extent.

It was, therefore, decided to limit the maximum phase shift to less than  $360^{\circ}$  by changing one of the series resonant circuits. With an optimized transformer, this circuit has the required performance.

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